Domagoj Jakobovic Faculty of Electrical Engineering and Computing, University of Zagreb Zagreb, Croatia domagoj.jakobovic@fer.hr Luca Manzoni Dipartimento di Matematica e Geoscienze, Università degli Studi di Trieste Trieste, Italy Imanzoni@units.it

Luca Mariot Cyber Security Research Group, Delft University of Technology Delft, The Netherlands l.mariot@tudelft.nl

Stjepan Picek Cyber Security Research Group, Delft University of Technology Delft, The Netherlands s.picek@tudelft.nl

# ABSTRACT

We investigate the use of Genetic Programming (GP) as a convolutional predictor for missing pixels in images. The training phase is performed by sweeping a sliding window over an image, where the pixels on the border represent the inputs of a GP tree. The output of the tree is taken as the predicted value for the central pixel. We consider two topologies for the sliding window, namely the Moore and the Von Neumann neighborhood. The best GP tree scoring the lowest prediction error over the training set is then used to predict the pixels in the test set. We experimentally assess our approach through two experiments. In the first one, we train a GP tree over a subset of 1000 complete images from the MNIST dataset. The results show that GP can learn the distribution of the pixels with respect to a simple baseline predictor, with no significant differences observed between the two neighborhoods. In the second experiment, we train a GP convolutional predictor on two degraded images, removing around 20% of their pixels. In this case, we observe that the Moore neighborhood works better, although the Von Neumann neighborhood allows for a larger training set.

# **CCS CONCEPTS**

• Computing methodologies → Image processing; Genetic programming; Bio-inspired approaches. KEYWORDS

#### KEI WORDS

Genetic Programming, Convolution, Supervised learning, Prediction, Images, Inpainting

#### ACM Reference Format:

Domagoj Jakobovic, Luca Manzoni, Luca Mariot, Stjepan Picek, and Mauro Castelli. 2021. CoInGP: Convolutional Inpainting with Genetic Programming. In 2021 Genetic and Evolutionary Computation Conference (GECCO

GECCO '21, July 10-14, 2021, Lille, France

© 2021 Association for Computing Machinery. ACM ISBN 978-1-4503-8350-9/21/07...\$15.00

https://doi.org/10.1145/3449639.3459346

Mauro Castelli NOVA Information Management School (NOVA IMS), Universidade Nova de Lisboa Lisbon, Portugal mcastelli@novaims.unl.pt

'21), July 10-14, 2021, Lille, France. ACM, New York, NY, USA, 9 pages. https://doi.org/10.1145/3449639.3459346

# **1 INTRODUCTION**

Nowadays, images represent a common testbed to evaluate the performance of many algorithms, especially those coming from the deep learning domain [5, 12, 14, 24]. The usability of images in this context is impaired if they are damaged or incomplete. Indeed, missing pixels can severely impact the information carried by the images and hinder the performances of artificial intelligence techniques trained on them. Hence, there is often the need to resort to image inpainting techniques. *Digital inpainting* generally denotes all methods related to the reconstruction of lost or damaged parts of an image by means of algorithms that replace such parts. We refer the reader to the recent surveys by Elharrous et al. [9] and Jam et al. [13] for a more complete overview of image inpainting techniques, while in the following, we recall only the essential approaches investigated in this research field.

Traditionally, two techniques have been explored for the image inpainting procedure. *Exemplar-based methods* fill a missing region by exploiting local information in the surrounding area. This can be done both at the level of single pixels, as in the pioneering work by Efros and Leung [8], or patch-wise, by searching for replacement patches in the parts of the image that are not damaged, as proposed for instance by Criminisi et al. [6]. On the other hand, in *diffusionbased techniques* inpainting is performed by spreading the image information from the boundary of a missing region towards its center, an approach that was initially investigated by Bertalmio et al. [2]. A further research thread also focused on combining both the exemplar-based and diffusion-based approaches by defining *hybrid methods*, as done for instance in [3].

More recently, *deep learning methods*, and in particular convolutional neural networks (CNNs), have shown excellent results on image inpainting tasks due to their ability to use large training sets [20]. The part where CNNs truly have an advantage over other inpainting techniques is the fact that they can better capture the global structure of an image [28]. Finally, researchers also used generative adversarial networks (GANs) for many image-to-image translation tasks, including image inpainting [12].

Permission to make digital or hard copies of all or part of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. Copyrights for components of this work owned by others than ACM must be honored. Abstracting with credit is permitted. To copy otherwise, or republish, to post on servers or to redistribute to lists, requires prior specific permission and/or a fee. Request permissions from permissions@acm.org.

When considering evolutionary algorithms, there are not many works examining the image inpainting task. Li et al. used a combination of a total variation method and a genetic algorithm for completing an image [18]. Li and Yang proposed a patch-based method based on evolutionary algorithms that search for the optimal patch in the area around the damaged region [19]. Interestingly, while convolutional neural networks represent state-of-the-art in image translation tasks, up to now, there are not many attempts to employ the convolutional paradigm in other artificial intelligence techniques. To the best of our knowledge, there is only a single work that considers how to combine convolutions and genetic programming [23]. There, the authors applied their method to develop image denoising filters with a multi-layer architecture.

This paper proposes a novel technique for the image inpainting task based on Genetic Programming (GP) [16] and convolutions. We denote our approach as CoInGP - Convolutional Inpainting with Genetic Programming. Our technique works locally by considering the immediate neighbors of a missing pixel, which are used as the input of a GP tree. The output evaluated at the root of the tree represents the predicted value for the central missing pixel. The window is then slid over the image, and the prediction process is repeated for the remaining missing pixels, thus obtaining a reconstructed image. We tackle the problem of evolving a suitable GP tree as a supervised learning task over known pixels. In particular, the training set is composed of fitness cases where the inputs are the values of the neighboring pixels for a specific position of the window, while the label corresponds to the correct value of the central pixel. The optimization objective consists in minimizing the RMSE between the predictions made by the GP tree and the correct labels over all fitness cases.

As far as we are aware, this is the first paper considering GP for image inpainting. Hence, more than comparing with state-of-theart deep learning methods such as CNNs and GANs (which we leave for future research), the main motivation of our work is to search for preliminary evidence that convolutional inpainting can also be performed with Genetic Programming as an underlying learning primitive. Incidentally, we adopted a similar approach in [21] for the domain of automatic text generation. For these reasons, we frame the investigation presented in this paper around two general research questions:

- (1) Can CoInGP learn the distribution of the pixels' intensities in a dataset of *complete* images?
- (2) Can CoInGP obtain a plausible reconstruction of a *single* degraded image by training on the available pixels?

For the first research question, we perform the training on a subset of 1000 images from the MNIST dataset [7] without missing pixels. The fitness of a GP tree in the population is evaluated by predicting the value of each pixel in all selected images (excluding those at borders, which do not have enough neighbors). The best evolved GP tree is then independently validated on another test set of 1000 complete images from MNIST. Concerning the second research question, we conduct an experiment on two different test images, where we remove around 20% of the pixels. In this case, the training is done on the available pixels, while the testing phase consists in predicting the actual missing pixels.

Domagoj Jakobovic, Luca Manzoni, Luca Mariot, Stjepan Picek, and Mauro Castelli

Further, we investigate a third research question that is orthogonal to the previous two: namely, whether the shape of the sliding window plays a role in the performance of GP when predicting the central pixel. To this end, we consider two different topologies for the window: *Moore neighborhood* and *Von Neumann neighborhood*.

Since this paper is mostly an empirical investigation of our approach's feasibility, in all our experiments, we compare the results obtained by CoInGP against those achieved by a simple baseline method, i.e., the predictor that computes the average value of the pixels in the neighborhood.

Our findings can be summarized as follows: regarding the first research question, GP is indeed able to learn the distribution of the pixels in a dataset of complete images to a certain extent, since for both neighborhood shapes, the evolved trees obtain a significantly lower RMSE than the respective baseline predictor. Moreover, in this case, we observe no statistically significant difference between Moore and Von Neumann neighborhoods. We obtain similar results for the second research question since CoInGP reaches a lower RMSE value than the baseline predictor when reconstructing the missing pixels of the two test images. However, in this case, there is a further difference between the two topologies considered for the sliding window, with Moore neighborhood achieving a better performance. This finding is especially interesting since, for geometrical reasons, Moore neighborhood can exploit a smaller training set than the Von Neumann neighborhood.

The rest of this paper is organized as follows. Section 2 formalizes the problem of predicting the central pixel in a sliding window by exploiting the information in the surrounding ones. Section 3 presents the details of our CoInGP method, showing how a GP tree can be used to predict an image's pixels and defining an appropriate fitness function to evaluate the quality of its predictions. Section 4 describes the experimental settings adopted in our empirical assessment of CoInGP and summarizes the obtained results. Section 5 gives an interpretation of the main experimental findings that can be drawn from our results and formulates some hypotheses worth exploring to investigate the observed behavior of CoInGP further. Finally, Section 6 recaps the main contributions of our paper and suggests future research directions on the subject.

# 2 PROBLEM FORMULATION

This section formalizes the problem of predicting pixels in an image, which will be tackled with genetic programming in the remainder of the paper. In what follows, we consider an input image as a matrix *I* of size  $M \times N$ , where each entry  $x_{(i,j)}$  is the intensity value of the pixel at coordinates (i, j) for  $i \in [M]$  and  $j \in [N]$ , where  $[M] = \{1, \dots, M\}$  and  $[N] = \{1, \dots, N\}$ . For illustration purposes, we deal only with 8-bit greyscale images, so that each entry  $x_{(i,j)}$  in the matrix is an integer number between 0 and 255; nevertheless, our approach can be generalized to any color depth.

Suppose that the image is *damaged*, that is, the intensities of a subset of k of its pixels  $S = \{(i_1, j_1), \dots, (i_k, j_k)\} \subseteq [M] \times [N]$  are missing. The goal is to recover the original intensities  $x_{(i_1,j_1)}, \dots, x_{(i_k,j_k)}$  starting from those that are still available, i.e., the pixels in the complementary set  $P = [M] \times [N] \setminus S$ . This task is also known as *inpainting* in the image processing literature [4, 11]. One of the possible approaches to perform inpainting stands on the fundamental

observation that the intensities of neighboring pixels are *correlated*. In a probabilistic framework, this property can also be restated as the fact that the probability distribution of a pixel's intensity given the intensities of the pixels in its neighborhood is independent of the rest of the image [8].

This observation suggests that, to recover the intensity of a missing pixel in an image, one can use just the values of its neighboring pixels as an input for the prediction. More formally, the two main topologies that can be adopted are the *Moore* neighborhood and the *Von Neumann* neighborhood [25]. Considering only neighborhoods of radius 1 (i.e., only the immediate neighbors of a pixels are taken into account), for the Moore neighborhood the input to predict a pixel in position (i, j) will be a 3 × 3 matrix defined as:

$$\mathcal{N}_{i,j} = \begin{bmatrix} x_{(i-1,j-1)} & x_{(i-1,j)} & x_{(i-1,j+1)} \\ x_{(i,j-1)} & x_{(i,j+1)} \\ x_{(i+1,j-1)} & x_{(i+1,j)} & x_{(i+1,j+1)} \end{bmatrix} , \qquad (1)$$

where the 8 elements on the border represent the intensities of the pixels in the neighborhoods, and the goal is to predict the value of the central pixel. Analogously, for a Von Neumann neighborhood the input to the prediction will be the following matrix:

$$\mathcal{N}_{i,j} = \begin{bmatrix} x_{(i-1,j)} & \\ x_{(i,j-1)} & x_{(i,j+1)} \\ & x_{(i+1,j)} \end{bmatrix} , \qquad (2)$$

where, in this case, we do not consider the elements in the corners and the input for predicting the central pixel are only the four elements which are respectively at its top, bottom, left, and right.

Intuitively, the quality of the prediction will also depend upon the number of available neighboring pixels: in particular, if also some of the neighboring pixels of  $N_{i,j}$  are missing in the degraded image, then we will have less information at our disposal to predict the central pixel  $x_{(i,j)}$ . In what follows, we adopt the simplifying assumption that each missing pixel in the degraded image is "sufficiently far" from all other missing pixels, or equivalently that each missing pixel has a complete neighborhood. Formally, in the case of Moore neighborhood this means that the *Chebyshev distance*  $d_{\infty}$ between any pair of missing pixels  $(i_{t_1}, j_{t_1}), (i_{t_2}, j_{t_2}) \in S$  must be strictly greater than 1:

$$d_{\infty}((i_{t_1}, j_{t_1}), (i_{t_2}, j_{t_2})) = \max\{|i_{t_1} - i_{t_2}|, |j_{t_1} - j_{t_2}|\} > 1$$

Analogously, for the Von Neumann neighborhood the constraint is that the *Manhattan distance*  $d_1$  between  $(i_{t_1}, j_{t_1})$  and  $(i_{t_2}, j_{t_2})$  has to be greater than 1:

$$d_1((i_{t_1}, j_{t_1}), (i_{t_2}, j_{t_2})) = |i_{t_1} - i_{t_2}| + |j_{t_1} - j_{t_2}| > 1 .$$

The consequence of these constraints is that missing pixels can share the frontier of the neighborhood under consideration, but a missing pixel cannot be in the *frontier* of another one. In particular, the frontier of a neighborhood of radius r is defined as the set of pixels at a distance r from the central one. Since we are only considering the case of radius r = 1, the frontier corresponds to the set of all pixels in the neighborhood except the central one. As an example, Figure 1 shows the densest packing of missing pixels one can have for the Moore and Von Neumann neighborhood, respectively. The Von Neumann topology allows for more missing pixels under the same image size since it includes fewer neighbors than the Moore topology. Also, observe that for both neighborhoods

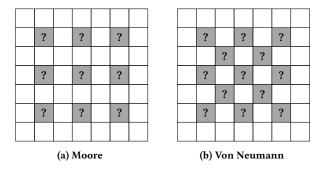


Figure 1: Densest packings of missing pixels allowed respectively under unitary Moore and Von Neumann neighborhoods.

the missing pixels cannot occur on the border of the image, i.e., 1 < i < M and 1 < j < N for every missing pixel  $(i, j) \in S$ .

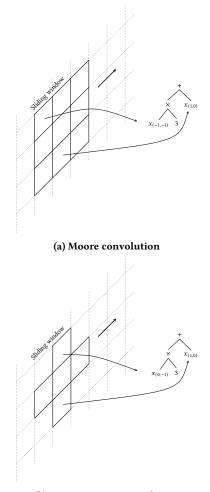
Although this separation hypothesis does not always hold in realistic scenarios, we decided to adopt it to initially validate the suitability of our method, since as we mentioned before, as far as we are aware, this is the first attempt employing GP to predict missing pixels in images with a convolutional approach.

#### **3 GP AS A CONVOLUTIONAL PREDICTOR**

The main idea that we investigate in this paper is to evolve GP trees that act as *convolutional operators* to predict the values of missing pixels. Similarly to what is done in *Convolutional Neural Networks* (CNNs) [10], we assume that the transformation used to predict the values of the missing pixels is *shift-invariant*. This means there is a *local function* f which is applied over a small *sliding window* of neighboring pixels and is shifted one place at a time over the whole image. The output of the function f corresponds to the predicted intensity of the pixel at the center of the window.

In our setting, we consider both the case of a square  $3 \times 3$  sliding window, which corresponds to the Moore neighborhood of radius 1, and a cross-shaped window of width 3, which represents the Von Neumann neighborhood of radius 1. In the former case, the local function has the form  $f : [0, 255]^8 \rightarrow [0, 255]$ , while in the latter it is  $f : [0, 255]^4 \rightarrow [0, 255]$ ; either way, the local function is expressed with a GP tree. Thus, the 8 (respectively, 4) intensities of the pixels on the border of the window are taken as terminal nodes of the GP tree, and the value generated at the root node will be the prediction for the central pixel. Figure 2 depicts the idea of using a GP tree as a convolutional predictor by sliding a window over the image for the case of Moore and Von Neumann neighborhoods.

To construct such a convolutional predictor, we need to define an appropriate fitness function that measures how good a particular GP tree is in determining the correct value for the central pixel. The idea is to frame the problem in terms of supervised learning, with the *training set* including fitness cases where the inputs are the values of the pixels in the neighborhood, and the labels are the correct values for the corresponding central pixel. Recall from Section 1 that we are interested in two research questions, which translates to the following tasks:



(b) Von Neumann convolution

Figure 2: Convolutional prediction based on GP with the Moore and Von Neumann neighborhood of radius 1. The pixels in the frontier of the neighborhood currently looked by the sliding window are fed as input variables to the GP tree, and its output is taken as the predicted value for the central pixel.

- (1) Given a set of complete images (i.e., without missing pixels) drawn from a common dataset, learn the distribution of the pixels' intensities in this set.
- (2) Given a *single* degraded image, reconstruct the complete image by predicting the values of the missing pixels.

For Task (1), let  $\mathcal{I} = \{I_1, \dots, I_n\}$  be a set of images, each of size  $M \times N$  and without missing pixels. For each image  $I_k$ , with  $k \in \{1, \dots, n\}$ , we define the corresponding *set of fitness cases* (or training examples) as follows:

$$F_k = \{ (\mathcal{N}_{i,j}, x_{(i,j)}) : 1 < i < M, 1 < j < M \} , \qquad (3)$$

where  $N_{i,j}$  is the punctured neighborhood matrix defined as in Eqs. (1) and (2), respectively when the Moore and Von Neumann neighborhood is used. In other words, for each pixel (i, j) in image

Domagoj Jakobovic, Luca Manzoni, Luca Mariot, Stjepan Picek, and Mauro Castelli

 $I_k$  (except for those on the borders), we construct the corresponding neighborhood matrix  $N_{i,j}$  (*without* the value of the pixel in the center) which is used as an input to a GP tree  $\tau$ . The actual intensity  $x_{i,j}$  of the central pixel (i, j) is retained as the correct label of the training example. The total number of fitness cases in  $F_k$  is thus (M-2)(N-2). Next, the global training set is defined as the union of the fitness cases sets of all images in I:

$$T_1 = \bigcup_{k=1}^n F_k \quad . \tag{4}$$

For Task (2), we consider a single degraded image *I* of size  $M \times N$ , where  $S = \{(i_1, j_1), \dots, (i_k, j_k)\}$  is the subset of missing pixels that satisfy respectively the Chebyshev distance  $d_{\infty} > 1$  constraint (if the Moore neighborhood is adopted) or the Manhattan distance  $d_1 > 1$  constraint (if the Von Neumann neighborhood is used). Further, let  $P = [M] \times [N] \setminus S$  be the complementary subset of available pixels. Then, the training set is defined as follows:

$$T_2 = \{ (\mathcal{N}_{i,j}, x_{(i,j)}) : (i,j) \in P, \ 1 < i < M, \ 1 < j < M \} \ .$$
 (5)

Hence,  $T_2$  is a particular case of Eq. (3), where the training examples are constrained only to the available pixels of the image having a complete neighborhood.

Given the output  $\hat{x}_{(i,j)} = \tau(N_{(i,j)})$ , we can compute the error that the GP tree  $\tau$  made in predicting the correct pixel intensity  $x_{(i,j)}$ . Generalizing to all available training examples, we define the fitness function for the GP tree  $\tau$  as the *root mean square error* (RMSE) over the training set:

$$fit(\tau) = \sqrt{\frac{\sum_{(N_{i,j}, x_{(i,j)}) \in T} (\tau(N_{i,j}) - x_{(i,j)})^2}{|T|}} \quad . \tag{6}$$

Hence, the optimization objective is to minimize fit, since having a GP tree that achieves a small RMSE means that its predictions are close to the actual pixel values. Observe that it is not necessary to specify the precise form of the training set in Eq. (6) depending on Task (1) or (2), since  $T_1$  simply concatenates the training examples of all images in the dataset I.

Once the GP evolution process has terminated, the best individual undergoes a *testing phase*. In Task (1), the best GP tree is used to predict the value of each pixel in all images of a test set  $\mathcal{T}$  different from I, although always drawn at random from the same dataset. Conversely, for Task (2), the best tree is used to predict the values of the pixels in the missing set S of the target image I. In both cases, the performance of the best tree is evaluated again with the RMSE measure. Clearly, in Task (2), this approach assumes that the missing set S can be artificially created to retain the original values of the pixels in it for computing the RMSE.

#### 4 EXPERIMENTAL PHASE

This section describes the experimental evaluation that we conducted to investigate the two research questions outlined in Section 1 through our CoInGP method. In what follows, we first discuss the common experimental settings and parameters adopted in our study. Then, we describe the setup and the results obtained for our two experiments, namely, learning the distribution of the pixels'

intensities for a set of complete images from the MNIST dataset and predicting the missing pixels in two degraded test images<sup>1</sup>.

## 4.1 Common Parameters

To experimentally assess our method, we loosely followed the GP parameter settings that we adopted in [21] for another supervised learning task, namely next word prediction, and checked with preliminary experiments that they were suitable for the image inpainting task as well. In particular, in each GP run, we evolved a population of 500 individuals for 500 generations, which amounts to 250 000 evaluations. The selection phase was performed using tournament selection with a tournament size of 3, where the worst individual is replaced by the offspring generated by applying crossover on the best two individuals. For the crossover, we adopted simple subtree, uniform, size fair, one-point, and context preserving crossover, randomly selected at each crossover operation. The newly generated individual undergoes a mutation subject to individual mutation probability of 0.3; we used a simple subtree mutation [22]. To avoid bloat, we set the maximum tree depth to 8, which corresponds to the number of input variables available in the Moore neighborhood. The terminal symbols for the GP trees included random constant values in the range [-1, 1] and either the 8 (for Moore neighborhood) or 4 (for Von Neumann neighborhood) input variables corresponding to the intensities of the available pixels in the respective neighborhood. The functional symbols for the internal nodes are taken from the following set: sin,  $\cos$ , +, -, / (protected), \*, min, max, avg,  $\sqrt{\cdot}$  and pos. The square root operator returns zero if the argument is negative, while the unary operator pos is defined as pos(x) = x if  $x \ge 0$  and 0 otherwise.

Since we require the predicted pixel intensity to be an integer number between 0 and 255, we constrained the output of a GP tree by first clipping it in the interval [0, 255] (i.e., if  $|\tau(N_{i,j})| > 255$  we set  $|\tau(N_{i,j})| = 255$ ), and then by applying a *linear scaling operator* to obtain the closest integer value, using the method proposed by Keijzer [15]. An alternative solution would be to directly use byteoriented operators in the functional set, such as bitwise logical operations, modular additions, and rotations. However, we deemed that this approach would have constrained too much the search space explored by GP, hindering its ability to generate good tree predictors with low RMSE fitness values.

#### 4.2 Experiments on the MNIST Dataset

For the first research question, we considered the well-known MNIST dataset [7], which contains images of handwritten digits. In particular, each image has a fixed size of  $28 \times 28$  pixels, with the digit placed at the center. For each experimental run, we randomly sampled from this dataset 1000 images for the training set, with the same number of images for each digit, and we constructed the corresponding training set  $T_1$  according to Eq. (4), and minimized the RMSE as defined in Eq. (6). In total, we performed 30 independent runs. At the end of each run, we validated the best GP tree with another random sample of 1000 images. The test set is still constructed using Eq. (4) and the performance criterion is the minimization of the fitness function. Thus, the idea is to verify

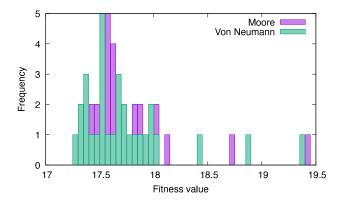


Figure 3: Histograms representing the distribution of the fitness values for the best individuals achieved in the same 30 independent runs, for both neighborhoods.

whether the GP tree resulting from the training phase can score a small RMSE on a set of unseen images.

The obtained results suggest that GP is indeed learning the distribution of the pixels in the training set. Indeed, the convergence of the best fitness during the training phase for the Moore and the Von Neumann neighborhoods showed that the RMSE decreased over all 30 experimental runs, thus indicating that the predicted pixels are closer and closer to their target values. The plot in Figure 3 shows the distribution of the fitness values, on the test set, for both Moore and Von Neumann neighborhood, over the 30 independent runs. To compare the results obtained on the test phase, we also computed the RMSE for the baseline predictors that replace the central pixel with the average value of the neighboring ones for the images. This resulted in an RMSE of 33.488 and 27.191 for the baseline predictors based on the Moore and the Von Neumann neighborhoods, respectively. Based on these results, one can observe that CoInGP is obtaining significantly better results than the baseline method in predicting the pixels over the test set since the RMSE values of the former are in the range 17.25 – 19.5 for both neighborhoods. Moreover, the overlapping of the two distributions indicates that the performance of CoInGP is not dependent on the neighborhood's choice. We further validated this qualitative observation through a statistical test. In particular, the Mann-Whitney test was executed (with a significance level of  $\alpha = 0.05$ ) under the null hypothesis that the median fitness of the two series of data (i.e., the one using Moore neighborhood and the one using Von Neumann neighborhood) were equal. The obtained p-value (0.6228) led us to not reject the null hypothesis, thus confirming that there is no difference between the two neighborhoods used by CoInGP.

The obtained results suggest the suitability of the proposed approach for the reconstruction of the damaged pixels of an image. The same results do not highlight a difference between the two neighborhood structures.

#### 4.3 Experiments on Single Images

To validate the previous findings in a more realistic scenario, the second part of the experimental phase applies the proposed approach to images that present a more complex pattern than the

 $<sup>^1{\</sup>rm The}$  source code of our implementation of CoInGP is publicly available at https://github.com/rymoah/CoInGP

GECCO '21, July 10-14, 2021, Lille, France



Figure 4: The damaged test images: Boat and Goldhill.

MNIST images. We employ two  $256 \times 256$  grayscale images on which approximately 20% of the pixels were removed. The two images (with the removed pixels) are presented in Figure 4.

We adopted the following procedure to generate the damaged images: every two columns of the image, the first one was kept unchanged while 100 non-adjacent pixels were randomly removed from the second. Overall, this procedure resulted in removing 12 700 pixels out of 65 536, corresponding to a percentage of removed pixels equal to 19.38% for each image. As detailed in Section 3, the training set T<sub>2</sub> used in this learning task is composed of all remaining pixels in the degraded image, along with their complete neighborhoods. Due to the different neighborhood shapes considered, the number of fitness cases for the Moore neighborhood was 4, 950, and for the Von Neumann neighborhood was 21, 036. That is, since the Von Neumann neighborhood contains fewer pixels, it also allows to employ a larger number of fitness cases. In this case, the training phase was performed for 100 independent runs. The testing is then performed by predicting the values of the removed pixels with the best GP individual at the end of each run, i.e., the one achieving the smaller RMSE over the training set.

The results of the reconstruction process are presented in Figure 5 for the Moore neighborhood, and in Figure 6 for the Von Neumann neighborhood. A closeup is presented in Figure 7.

The reconstructed images are both taken from a random GP run. For each image, we also present the pixel-by-pixel difference between the reconstructed image and the original one, where each difference is increased ten times to make it visible. As it is possible to observe, the errors in both cases are limited (i.e., there are no extremely different pixels) and distributed mainly across the edges of the objects in the image. This is particularly visible in the Boat image, where the distribution of the error mostly follows the profiles of the hull and the masts.

Besides qualitative considerations on the reconstructed images, we also assessed whether CoInGP could predict missing pixels in these images from a quantitative point of view, performing again a comparison with the baseline predictors that compute the average intensities of the neighboring pixels. Figure 8 depicts the plots of the distributions of the best fitness over 100 experimental runs achieved by GP over each test image.

As a general remark, in most cases, all fitness values obtained are below both baselines, independently of the underlying neighborhood. The only exceptions which occur, however, are limited to a few outliers. In particular, some runs in the distribution of Domagoj Jakobovic, Luca Manzoni, Luca Mariot, Stjepan Picek, and Mauro Castelli



Figure 5: At the top, the images corrected using the Moore neighborhood. At the bottom, the difference, increased ten times, between the reconstructed and the original image.



Figure 6: At the top, the images corrected using the Von Neumann neighborhood. At the bottom, the difference, increased ten times, between the reconstructed and the original image.

the Moore neighborhood scored an RMSE value between the two baselines, while a small part of the right tail of the Von Neumann distribution overlaps the corresponding baseline in the Goldhill

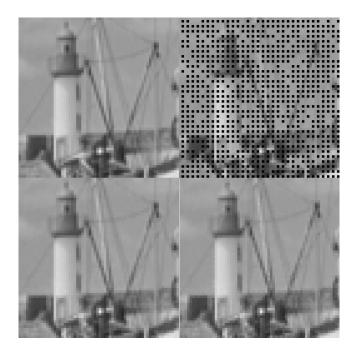


Figure 7: A closeup of the correction performed by GP on one of the images. Clockwise from the top left: original image, damaged image, corrected images with the Von Neumann and Moore neighbourhoods, respectively.

image. In any case, we noticed that the peaks of all GP distributions are significantly distant from the respective baseline fitness values. Further, in all the test images, the use of the Moore neighborhood produces lower fitness values than the Von Neumann neighborhood, even if it allows fewer training samples to be generated.

## 5 DISCUSSION

We now interpret the experimental results reported in the previous section in the light of the two research questions stated in Section 1. Regarding the first question, we can empirically conclude that our CoInGP method can successfully learn the distribution of the pixels' intensities in a dataset of complete images, i.e., without missing pixels. Indeed, the convergence plots for the best fitness during the training phase on the MNIST dataset show that the evolutionary process implemented by GP is learning how to minimize the error between the correct label for the central pixel in the window and the predicted one. The distributions of the best fitness on the test set confirm that GP can generalize to unseen images to a certain extent, and a comparison with the baseline predictors shows that it achieves a significantly lower RMSE.

Concerning the second research question, in our experimental setting, the missing pixels accounted for roughly 20% of the pixels of each test image. Our approach's main limitation is that the training process requires a complete neighborhood, i.e., no missing pixels must occur in the frontier of the central pixel whose value has to be predicted. This limits both the number of missing pixels that one can have in the degraded image and their relative positions. However, the preliminary results that we obtained on the test

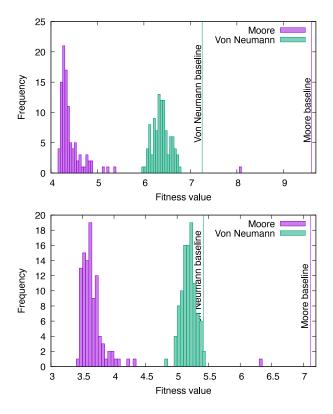


Figure 8: Distribution of best fitness over 100 runs with both Moore and Von Neumann neighborhoods for the Boat image (top plot) and the Goldhill image (bottom plot).

images are promising enough to encourage further improvements in this direction by extending our method to consider the case of *adjacent* missing pixels in the degraded image. An interesting idea to accomplish this task could be to employ a diffusion-based inpainting approach [17]. In this case, the GP predictor would be first convolved on the border of a missing region and then gradually shifted towards its interior.

An interesting difference that can be remarked between the two experiments regards the influence of the sliding window's topology on the performance of CoInGP. In fact, for the MNIST experiment, we detected no significant difference between the Moore and Von Neumann neighborhoods, suggesting that this parameter is not a key factor when learning the distribution of pixels of complete images. Conversely, when going into the details of the second experiment with a single test image, the GP predictors based on the Moore neighborhood achieved a better performance (i.e., a lower RMSE value) than those using the Von Neumann neighborhood. This happens even though the Von Neumann neighborhood requires fewer input variables to compute the predicted missing pixel and can be optimized on a larger training set. Consequently, this result indicates that GP can learn more efficiently by using a larger number of input variables and a smaller training set. It would be interesting to investigate if this difference in terms of performance also holds for larger neighborhoods. Still, for radius 2, this would already yield GP trees with 24 and 12 input variables, respectively,

for the Moore and Von Neumann neighborhood, thereby increasing both the training time and the GP predictors size.

Recall that the baseline predictors simply computed the average of the pixels in the neighborhood to predict the value of the central one. An interesting fact that can be observed from our experiments is that the RMSE achieved by the Von Neumann baseline predictor is lower than that scored by the Moore baseline, both in the MNIST dataset and the single test images. Hence, this suggests that the information for predicting the central pixel is not uniformly distributed across the neighboring ones: it seems that the 4 "diagonal" pixels in the Moore neighborhood contain less information to predict the central one. Nonetheless, this observation is in stark contrast with the fact that GP scored a lower RMSE value with the Moore neighborhood than with the Von Neumann neighborhood. This indicates that CoInGP can learn how to correctly "weigh" the value of the pixels depending on their position. It would be interesting to further investigate this issue by analyzing the structure of the trees evolved by GP with the Moore neighborhood.

Finally, from the qualitative point of view, we observed that the prediction errors made by GP individuals mostly focused around the edges in the test images. This is an expected side effect: if one considers images as two-dimensional spatial signals, edges correspond to high-frequency regions, where abrupt changes of the intensity value occur among neighboring pixels. Consequently, the pixels' intensities in a neighborhood where an edge occurs have a lower correlation. Additionally, the independence hypothesis that the probability distribution of a pixel given the surrounding ones is independent of the rest of the image does not hold. This explains why our GP convolutional predictor obtains a higher error on edges' proximity, but it is not necessarily a negative effect: one could use CoInGP to perform edge detection as a by-product. Furthermore, an interesting idea to decrease the prediction error on the edges would be to develop a 2-layer architecture: the first layer would be used to detect the edges, while the second one would perform the inpainting task by discriminating between pixels' types. For the latter case, one could evolve GP trees over a larger neighborhood so that more information can be used to predict the central pixel.

## 6 CONCLUSIONS AND FUTURE WORK

In this paper, we proposed a method for performing convolutional inpainting with GP – CoInGP. The main idea is to sweep a small sliding window over a degraded image with missing pixels, where the neighborhood pixels captured by the window are fed as input to a GP tree. The GP's output is then taken as the predicted value for the central pixel. The RMSE between the original pixel intensities and those predicted by the GP tree is used to define a fitness function, which has to be minimized. We investigated this approach through two research questions, namely whether GP can learn the distribution of the pixels' intensities from a dataset of complete images and whether GP can restore a plausible reconstructed version of a single degraded image with missing pixels. To this end, we carried out two supervised learning experiments.

In the first experiment, the training set is composed of a random sample of 1000 images from the MNIST dataset, with the objective of minimizing the RMSE over all pixels of each image. The best GP tree evolved during this phase is then validated by applying it over a distinct test set. The results showed that our CoInGP method was able to generalize to a certain extent on unseen images since it performed better than the respective baseline predictors. Moreover, no difference was observed between using a sliding window with the Moore neighborhood and the Von Neumann neighborhood.

In the second experiment, given a degraded image with missing pixels, an optimal GP tree predictor is evolved by using all available pixels as a training set. For each position of the sliding window, the central pixel is removed and replaced with the value predicted by a GP tree. The test phase consists in applying the best tree evolved by GP on the actual missing pixels. We experimented with two test images. The results showed that GP could evolve trees with better prediction accuracy than the respective baseline predictor. Furthermore, in this case, we observed a clear difference in terms of performance between the Moore and the Von Neumann neighborhood, with the former achieving lower RMSE scores than the latter on the test sets. Considering that the Von Neumann baseline predictor has a lower RMSE than the Moore one, this seems to suggest that GP can learn how to appropriately assess the information contained in the pixels at the corners of the Moore neighborhood.

We conclude by pointing out directions for future research besides those already discussed in the previous section. The experiments presented in this paper suggest that using GP as a convolutional predictor represents an interesting building block to be plugged in more complex architectures for supervised learning tasks in the image domain. We sketched the first idea of this approach in Section 5, where we proposed to use a first GP convolutional layer for detecting the edges in an image and then use the second layer to perform inpainting. Thus, it would be interesting to generalize this concept to multiple GP-based convolutional layers and see how the performance of the overall system compares to other analogous and more established methods (i.e., like CNNs). Besides the inpainting technique, one could also consider the application of GP to other image processing tasks that can be formulated as supervised learning problems. This includes not only tasks where the training has to be performed on a single target image, as in the inpainting case, but also on multiple images, such as image classification. In particular, this would likely benefit from the use of a multi-layered architecture where each GP-based convolutional layer would be used to extract a particular feature of an image.

Finally, the convolution strategy is general enough to be applied to any kind of learning task in the signal processing domain. In this paper, we addressed the use case of images, which can be considered as two-dimensional spatial signals, but it could be interesting to explore how convolutional GP behaves on one-dimensional signals such as time series. In particular, the problem of predicting missing data in general signals is also known as *imputation*, which is useful for symbolic regression over incomplete datasets. As far as we know, there are a few works in the literature addressing the imputation problem using GP [1, 26, 27], but none of them uses a convolutional approach like the one proposed in this paper.

# ACKNOWLEDGMENTS

Mauro Castelli acknowledges financial support from Fundação para a Ciência e a Tecnologia (award number: DSAIPA/DS/0022/2018) and from the Slovenian Research Agency (award number: P5-0410).

#### GECCO '21, July 10-14, 2021, Lille, France

### REFERENCES

- [1] Baligh Al-Helali, Qi Chen, Bing Xue, and Mengjie Zhang. 2020. Hessian Complexity Measure for Genetic Programming-Based Imputation Predictor Selection in Symbolic Regression with Incomplete Data. In Genetic Programming - 23rd European Conference, EuroGP 2020, Held as Part of EvoStar 2020, Seville, Spain, April 15-17, 2020, Proceedings. 1–17.
- [2] Marcelo Bertalmío, Guillermo Sapiro, Vicent Caselles, and Coloma Ballester. 2000. Image inpainting. In Proceedings of the 27th Annual Conference on Computer Graphics and Interactive Techniques, SIGGRAPH 2000, New Orleans, LA, USA, July 23-28, 2000, Judith R. Brown and Kurt Akeley (Eds.). ACM, 417–424.
- [3] Marcelo Bertalmío, Luminita A. Vese, Guillermo Sapiro, and Stanley J. Osher. 2003. Simultaneous structure and texture image inpainting. *IEEE Trans. Image Process.* 12, 8 (2003), 882–889.
- [4] Aurélie Bugeau, Marcelo Bertalmío, Vicent Caselles, and Guillermo Sapiro. 2010. A Comprehensive Framework for Image Inpainting. *IEEE Trans. Image Processing* 19, 10 (2010), 2634–2645.
- [5] Chaofan Chen, Oscar Li, Daniel Tao, Alina Barnett, Cynthia Rudin, and Jonathan Su. 2019. This Looks Like That: Deep Learning for Interpretable Image Recognition. In Advances in Neural Information Processing Systems 32: Annual Conference on Neural Information Processing Systems 2019, NeurIPS 2019, 8-14 December 2019, Vancouver, BC, Canada. 8928–8939.
- [6] Antonio Criminisi, Patrick Pérez, and Kentaro Toyama. 2004. Region filling and object removal by exemplar-based image inpainting. *IEEE Trans. Image Process.* 13, 9 (2004), 1200–1212.
- [7] Li Deng. 2012. The mnist database of handwritten digit images for machine learning research [best of the web]. *IEEE Signal Processing Magazine* 29, 6 (2012), 141–142.
- [8] Alexei A. Efros and Thomas K. Leung. 1999. Texture Synthesis by Non-parametric Sampling. In Proceedings of the International Conference on Computer Vision, Kerkyra, Corfu, Greece, September 20-25, 1999. 1033–1038.
- [9] Omar Elharrouss, Noor Almaadeed, Somaya Al-Máadeed, and Younes Akbari. 2020. Image Inpainting: A Review. *Neural Process. Lett.* 51, 2 (2020), 2007–2028.
- [10] Ian Goodfellow, Yoshua Bengio, and Aaron Courville. 2016. Deep Learning. MIT Press. http://www.deeplearningbook.org.
  [11] Christine Guillemot and Olivier Le Meur. 2014. Image Inpainting : Overview and
- [11] Christine Guillemot and Olivier Le Meur. 2014. Image Inpainting : Overview and Recent Advances. IEEE Signal Process. Mag. 31, 1 (2014), 127–144.
- [12] Phillip Isola, Jun-Yan Zhu, Tinghui Zhou, and Alexei A. Efros. 2017. Image-to-Image Translation with Conditional Adversarial Networks. In 2017 IEEE Conference on Computer Vision and Pattern Recognition, CVPR 2017, Honolulu, HI, USA, July 21-26, 2017. 5967–5976.
- [13] Jiréh Jam, Connah Kendrick, Kevin Walker, Vincent Drouard, Gee-Sern Jison Hsu, and Moi Hoon Yap. 2021. A comprehensive review of past and present image inpainting methods. *Comput. Vis. Image Underst.* 203 (2021), 103147.
- [14] Jonathan Janke, Mauro Castelli, and Aleš Popovič. 2019. Analysis of the proficiency of fully connected neural networks in the process of classifying digital images. Benchmark of different classification algorithms on high-level image features from convolutional layers. *Expert Systems with Applications* 135 (2019), 12–38.

- [15] Maarten Keijzer. 2003. Improving Symbolic Regression with Interval Arithmetic and Linear Scaling. In Genetic Programming, 6th European Conference, EuroGP 2003, Essex, UK, April 14-16, 2003. Proceedings. 70–82.
- [16] John R. Koza. 1992. Genetic Programming: On the Programming of Computers by Means of Natural Selection. MIT Press, Cambridge, MA, USA.
- [17] H. Li, W. Luo, and J. Huang. 2017. Localization of Diffusion-Based Inpainting in Digital Images. *IEEE Transactions on Information Forensics and Security* 12, 12 (2017), 3050–3064.
- [18] Kangshun Li, Yunshan Wei, Zhen Yang, and Wenhua Wei. 2016. Image inpainting algorithm based on TV model and evolutionary algorithm. *Soft Computing* 20 (2016), 885–893.
- [19] K. Li and Z. Yang. 2013. Exemplar Image Completion Based on Evolutionary Algorithms. In 2013 Fourth International Conference on Emerging Intelligent Data and Web Technologies. 696–701.
- [20] Guilin Liu, Fitsum A. Reda, Kevin J. Shih, Ting-Chun Wang, Andrew Tao, and Bryan Catanzaro. 2018. Image Inpainting for Irregular Holes Using Partial Convolutions. In Computer Vision - ECCV 2018 - 15th European Conference, Munich, Germany, September 8-14, 2018, Proceedings, Part XI (Lecture Notes in Computer Science), Vittorio Ferrari, Martial Hebert, Cristian Sminchisescu, and Yair Weiss (Eds.), Vol. 11215. Springer, 89-105.
- [21] Luca Manzoni, Domagoj Jakobovic, Luca Mariot, Stjepan Picek, and Mauro Castelli. 2020. Towards an evolutionary-based approach for natural language processing. In GECCO '20: Genetic and Evolutionary Computation Conference, Cancún Mexico, July 8-12, 2020, Carlos Artemio Coello Coello (Ed.). ACM, 985–993.
- [22] Riccardo Poli, William B. Langdon, and Nicholas Freitag McPhee. 2008. A Field Guide to Genetic Programming. lulu.com.
- [23] Lino Rodriguez-Coayahuitl, Alicia Morales-Reyes, and Hugo Jair Escalante. 2019. Convolutional Genetic Programming. In *Pattern Recognition*, Jesús Ariel Carrasco-Ochoa, José Francisco Martínez-Trinidad, José Arturo Olvera-López, and Joaquín Salas (Eds.). Springer International Publishing, Cham, 47–57.
- [24] Olga Russakovsky, Jia Deng, Hao Su, Jonathan Krause, Sanjeev Satheesh, Sean Ma, Zhiheng Huang, Andrej Karpathy, Aditya Khosla, Michael Bernstein, Alexander C. Berg, and Li Fei-Fei. 2015. ImageNet Large Scale Visual Recognition Challenge. International Journal of Computer Vision (IJCV) 115, 3 (2015), 211–252.
- [25] Joel L Schiff. 2011. Cellular automata: a discrete view of the world. Vol. 45. John Wiley & Sons.
- [26] Cao Truong Tran, Mengjie Zhang, and Peter Andreae. 2015. Multiple Imputation for Missing Data Using Genetic Programming. In Proceedings of the Genetic and Evolutionary Computation Conference, GECCO 2015, Madrid, Spain, July 11-15, 2015. 583–590.
- [27] Cao Truong Tran, Mengjie Zhang, Peter Andreae, and Bing Xue. 2017. Multiple imputation and genetic programming for classification with incomplete data. In Proceedings of the Genetic and Evolutionary Computation Conference, GECCO 2017, Berlin, Germany, July 15-19, 2017. 521–528.
- [28] Zhaoyi Yan, Xiaoming Li, Mu Li, Wangmeng Zuo, and Shiguang Shan. 2018. Shift-Net: Image Inpainting via Deep Feature Rearrangement. In *Computer Vision – ECCV 2018*, Vittorio Ferrari, Martial Hebert, Cristian Sminchisescu, and Yair Weiss (Eds.). Springer International Publishing, Cham, 3–19.